

Dimensional Analysis

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Definition: A tool used to convert given units into other units. Phyllis Payne calls this technique multiplying by “a name for one”.

Example: *How many feet are in a 5.00 kilometer race?*

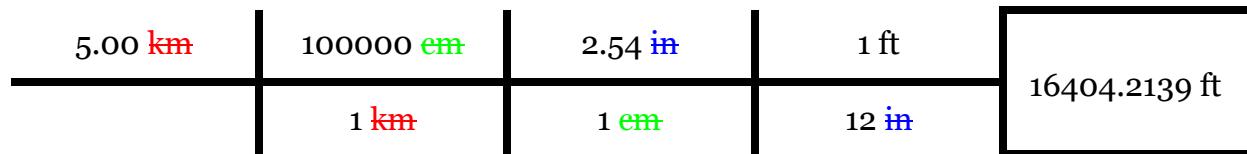
Conversions: $1 \text{ km} = 100000 \text{ cm}$

$$1 \text{ cm} = 2.54 \text{ in}^*$$

$$12 \text{ in} = 1 \text{ ft}$$

So long as these are equal, the symmetric property of equality holds true. In other words, you can “flip” the fractions around to get the dimensions to cancel.

Solution:



BUT WAIT! THERE'S MORE! We have given an absurdly long number of significant figures. Using dimensional analysis, we treat every definition as having an *infinite* number of sig figs. Therefore our answer should have 3 sig figs because 5.00 km is the value with the least number of sig figs.

Answer: There are 16400 ft in 5.00 km.

Side Note: As a class, let's collectively decide to not call this “train tracks” because

1. It looks nothing like real train tracks.
2. It sounds stupid and brings down the IQ of the whole class.

* In 1959 the inch became defined as 2.540005 cm after the U.S. yard was defined as 0.9144018 meters. However, 2.54 cm has been universally recognised as the definition of one inch.